

# 11. [Percentages]

## Skill 11.1 Writing a number out of 100 as a percentage.

MM4.2 1 2 2 3 3 4 4  
MM5.1 1 1 2 2 3 3 4 4

- Write the number followed by the percent symbol “%”  
Hint: “Percentage” means “per hundred” or “of each hundred”.

**Q.** Write as a percentage:  
84 out of 100.

**A.** 84 out of 100 =  
= **84%**

**a)** Write as a percentage:  
60 out of 100.

60%

**b)** Write as a percentage:  
32 out of 100.

**c)** Write as a percentage:  
46 out of 100.

**d)** Write as a percentage:  
12 out of 100.

**e)** Write as a percentage:  
5 out of 100.

**f)** Write as a percentage:  
9 out of 100.

**g)** Write as a percentage:  
61 out of 100.

**h)** Write as a percentage:  
53 out of 100.

**i)** Write as a percentage:  
4 out of 100.

**j)** Write as a percentage:  
7 out of 100.

**k)** Write as a percentage:  
59 out of 100.

**l)** Write as a percentage:  
91 out of 100.

**m)** Write as a percentage:  
28 out of 100.

**n)** Write as a percentage:  
79 out of 100.

- Subtract the given percentages from 100%, to find the remaining percentage.

**Q.** According to a projection for 2020, 39% of the population of the USA will be aged between 0 - 29 and 35% between 30 - 59. What percentage of the population will be aged 60 or more?

$$\begin{aligned} \text{A. } & 100\% - 39\% - 35\% \\ & = 100\% - 74\% \\ & = \mathbf{26\%} \end{aligned}$$

**a)** Approximately 59% of the athletes at the 2000 Sydney Olympics were male. What percentage of the athletes were female?

$$100\% - 59\% = \boxed{41\%}$$

**b)** School is approximately 60% of the calendar year in the Russian Federation. What percentage do holidays account for?

$$100\% - 60\% = \boxed{\phantom{00\%}}$$

**c)** The green-yellow 18-carat gold is 75% gold and the rest is silver. What percentage is silver?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**d)** If 89% of the West Point military academy graduates are male, what percentage are females?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**e)** If 78% of the Supreme Court justices are male, what percentage are females?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**f)** If the cucumber is 96% water, what percentage do the other components equal?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**g)** In Mali 72% of people earn less than \$1 a day. What percentage of people earn more than \$1 a day?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**h)** If 37.5% of the adult teeth are incisors and canines, what percentage is formed by molars and pre-molars?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**i)** Approximately 60.5% of the world population lives in Asia and 13.5% lives in North and South America. What percentage of the population lives in the rest of the world?

$$100\% - 60.5\% - 13.5\% = \boxed{\phantom{00\%}}$$

**j)** Approximately 27.2% of the world population is aged between 0 and 14 years and 65.2% between 15 and 64 years. What percentage of the population is aged 65 years and over?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**k)** If England occupies 57% and Scotland occupies 34% of Great Britain (the main island of the United Kingdom), what percentage is occupied by Wales?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

**l)** At the 2012 London Olympics, 20% of the medals won by Australia were gold, and 46% were silver. What percentage of the medals were bronze?

$$\dots\dots\dots = \boxed{\phantom{00\%}}$$

### Skill 11.3 Finding a percentage of multiples of 100 (1).

MM4.2 11 22 33 44  
MM5.1 11 22 33 44

**EITHER**

- Change the percentage to a fraction out of 100.

Example:  $40\% = \frac{40}{100}$

- Rewrite the question as a multiplication (change “of” to “×”).
- Change the whole number to a fraction over 1.

Example:  $7 = \frac{7}{1}$

- Cross simplify the fractions before multiplying. (see skill 10.4, page 60)

**OR**

- First find 10%.
- Then multiply by the amount needed to make the required percentage, i.e. multiply by 3 to get 30%.

To find  $10\% = \frac{1}{10} \Rightarrow$  divide by 10  
 $5\% \Rightarrow$  half of 10%  
 $20\% = \frac{1}{5} \Rightarrow$  divide by 5  
 $25\% = \frac{1}{4} \Rightarrow$  divide by 4  
 $50\% = \frac{1}{2} \Rightarrow$  divide by 2

**Q.**  $40\%$  of \$6.00 =

**A.**  $40\%$  of \$6.00 =  $40\%$  of 600 *Convert \$ to cents*  
 $= \frac{40}{100} \times \frac{600}{1}$  *Simplify: ÷ 100*  
 $= 40 \times 6$   
 $= 240$  cents  
 $= \$2.40$

**OR A.**  $600 \div 10 = 60$  *Find 10%*  
 $= 60$  cents  
 $60 \times 4 = 240$  *Multiply by 4 to get 40%*  
 $= 240$  cents  
 $= \$2.40$

**a)**  $24\%$  of 100 =  $\frac{24}{100} \times \frac{100}{1} = 24$  *Divide by 100*

**b)**  $85\%$  of 100 =  $\frac{85}{100} \times \frac{100}{1} = 85$

**c)**  $69\%$  of 100 =  $\frac{69}{100} \times \frac{100}{1} = 69$

**d)**  $9\%$  of \$100 =  $\frac{9}{100} \times \frac{100}{1} = 9$  \$

**e)**  $7\%$  of \$100 =  $\frac{7}{100} \times \frac{100}{1} = 7$  \$

**f)**  $50\%$  of \$100 =  $\frac{50}{100} \times \frac{100}{1} = 50$  \$

**g)**  $75\%$  of \$400 =  $\frac{75}{100} \times \frac{400}{1} = 75 \times 4 = 300$  \$

**h)**  $10\%$  of \$300 =  $\frac{10}{100} \times \frac{300}{1} = 30$  *Divide 300 by 10* \$

**i)**  $30\%$  of \$500 =  $\frac{30}{100} \times \frac{500}{1} = 30 \times 5 = 150$  *Find 10% first* \$

**j)**  $60\%$  of \$200 =  $\frac{60}{100} \times \frac{200}{1} = 60 \times 2 = 120$  \$

**k)**  $25\%$  of \$800 =  $\frac{25}{100} \times \frac{800}{1} = 25 \times 8 = 200$  \$

**l)**  $70\%$  of \$600 =  $\frac{70}{100} \times \frac{600}{1} = 70 \times 6 = 420$  \$

Skill 11.3 Finding a percentage of multiples of 100 (2).

m) 5% of \$300 =

$$= \frac{5}{100} \times \frac{300}{1}$$

$$= 5 \times 3 = \$ \boxed{\phantom{00}}$$

n) 5% of \$500 =

$$500 \div 10 = 50$$

$$50 \div 2 = \$ \boxed{\phantom{00}}$$

o) 5% of \$700 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

p) 50% of \$700 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

q) 20% of \$200 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

r) 40% of \$500 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

s) 80% of \$400 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

t) 90% of \$300 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

u) 15% of \$400 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

v) 50% of \$5.00 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

w) 20% of \$3.00 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

x) 75% of \$6.00 =

$$= \phantom{00} = \$ \boxed{\phantom{00}}$$

y) 5% of \$4.00 =

$$= \phantom{00} = \boxed{\phantom{00}} \text{ ¢}$$

z) 40% of \$3.50 =

$$= \phantom{00} = \boxed{\phantom{00}} \text{ ¢}$$

A) 30% of \$4.50 =

$$= \phantom{00} = \boxed{\phantom{00}} \text{ ¢}$$

# Skill 11.4 Finding a percentage of any number (1).

## EITHER

- Change the percentage to a fraction out of 100.

Example:  $40\% = \frac{40}{100}$

- Rewrite the question as a multiplication (change "of" to "×").
- Change the whole number to a fraction over 1.

Example:  $7 = \frac{7}{1}$

- Cross simplify the fractions before multiplying. (see skill 10.4, page 60)

## OR

- First find 10%.
- Then multiply by the amount needed to make the required percentage, i.e. multiply by 3 to get 30%.

To find  $1\% = \frac{1}{100} \Rightarrow$  divide by 100  
 $12.5\% = \frac{1}{8} \Rightarrow$  divide by 8  
 $33\frac{1}{3}\% = \frac{1}{3} \Rightarrow$  divide by 3  
 $66\frac{2}{3}\% = \frac{2}{3} \Rightarrow$  divide by 3  
 multiply by 2

**Q.**  $66\frac{2}{3}\%$  of 270 =

**A.**  $66\frac{2}{3}\%$  of 270 =  
 $= \frac{2}{3} \times \frac{270}{1}$  *Simplify: ÷ 3*  
 $= 2 \times 90$   
 $= 180$

Substitute  $66\frac{2}{3}\%$  with  $\frac{2}{3}$   
 Change "of" to "×"  
 Change 270 to  $\frac{270}{1}$   
 Multiply  $\frac{2}{3}$  by  $\frac{270}{1}$

**a)** 20% of 50 =  
 $= \frac{20}{100} \times \frac{50}{1}$  *Simplify: ÷ 10, twice*  
 $= 2 \times 5 = 10$

**b)** 70% of 240 = *Find 10% first*  
 $240 \div 10 = 24$   
 $24 \times 7 =$  *Multiply by 7 to get 70%*

**c)** 80% of 20 =  
 =  
 =

**d)** 40% of 80 =  
 =  
 =

**e)** 60% of 250 =  
 =  
 =

**f)** 30% of 140 =  
 =  
 =

**g)** 70% of 120 =  
 =  
 =

**h)** 5% of 40 =  
 =  
 =

**i)** 5% of 120 =  
 =  
 =

**j)** 15% of 60 = *Find 10% first*  
 10%  $60 \div 10 = 6$   
 5%  $6 \div 2 = 3$  *5% is half of 10%*  
 15%  $6 + 3 =$

**k)** 35% of 80 =  
 =  
 =

**l)** 45% of 120 =  
 =  
 =

m) 25% of 180 =

$$= \frac{25}{100} \times \frac{180}{1}$$

Simplify:  $\div 5$

$$= \frac{90}{2} = \boxed{\phantom{00}}$$

Divide by 10

n) 75% of 40 =

$$= \frac{75}{100} \times \frac{40}{1}$$

$$= \frac{300}{100} = \boxed{\phantom{00}}$$

o) 75% of 120 =

$$= \frac{75}{100} \times \frac{120}{1}$$

$$= \frac{9000}{100} = \boxed{\phantom{00}}$$

p) 15% of 40 =

$$= \frac{15}{100} \times \frac{40}{1}$$

Simplify:  $\div 10$

$$= \frac{60}{10} = \boxed{\phantom{00}}$$

q) 6% of 30 =

$$= \frac{6}{100} \times \frac{30}{1}$$

$$= \frac{180}{100} = \boxed{\phantom{00}}$$

r) 8% of 80 =

$$= \frac{8}{100} \times \frac{80}{1}$$

$$= \frac{640}{100} = \boxed{\phantom{00}}$$

s) 1% of 300 =

$$= \frac{1}{100} \times \frac{300}{1}$$

$$= \frac{300}{100} = \boxed{\phantom{00}}$$

t) 1% of 150 =

$$= \frac{1}{100} \times \frac{150}{1}$$

$$= \frac{150}{100} = \boxed{\phantom{00}}$$

u) 2% of 50 =

$$= \frac{2}{100} \times \frac{50}{1}$$

$$= \frac{100}{100} = \boxed{\phantom{00}}$$

v) 12.5% of 560 =

$$= \frac{12.5}{100} \times \frac{560}{1}$$

Simplify:  $\div 8$

$$= \frac{7000}{80} = \boxed{\phantom{00}}$$

w) 12.5% of 80 =

$$= \frac{12.5}{100} \times \frac{80}{1}$$

$$= \frac{1000}{80} = \boxed{\phantom{00}}$$

x) 12.5% of 160 =

$$= \frac{12.5}{100} \times \frac{160}{1}$$

$$= \frac{2000}{80} = \boxed{\phantom{00}}$$

y)  $33\frac{1}{3}\%$  of 150 =

$$= \frac{1}{3} \times \frac{150}{1}$$

Simplify:  $\div 3$

$$= \frac{150}{3} = \boxed{\phantom{00}}$$

z)  $33\frac{1}{3}\%$  of 180 =

$$= \frac{1}{3} \times \frac{180}{1}$$

$$= \frac{180}{3} = \boxed{\phantom{00}}$$

A)  $33\frac{1}{3}\%$  of 60 =

$$= \frac{1}{3} \times \frac{60}{1}$$

$$= \frac{60}{3} = \boxed{\phantom{00}}$$

B)  $66\frac{2}{3}\%$  of 90 =

$$= \frac{2}{3} \times \frac{90}{1}$$

$$= \frac{180}{3} = \boxed{\phantom{00}}$$

C)  $66\frac{2}{3}\%$  of 150 =

$$= \frac{2}{3} \times \frac{150}{1}$$

$$= \frac{300}{3} = \boxed{\phantom{00}}$$

D)  $66\frac{2}{3}\%$  of 210 =

$$= \frac{2}{3} \times \frac{210}{1}$$

$$= \frac{420}{3} = \boxed{\phantom{00}}$$

**To find the discount on an item**

- Calculate the percentage of the given amount. (see skill 11.3, page 69 and skill 11.4, page 71)  
Discount is associated with words like: *discounted, reduced, off, save, cash back*

**To find the sale price if a discount is applied**

- Calculate the percentage of the given amount.
- Subtract this result from the given amount.

**Q.** In a store a \$300 jacket is marked '20% off'. What is the sale price of the jacket?

**A.** *Discount:* 20% of 300 =

$$= \frac{20}{100} \times \frac{300}{1} \quad \text{Divide by 100}$$

$$= 20 \times 3 = 60$$

*Sale price:* 300 - 60 = **\$240**

**a)** If a \$30 T-shirt is reduced by 15%, what is the discount?

*discount:* 15% of 30 =

$$= \frac{15}{100} \times \frac{30}{1} = \frac{45}{10} = \boxed{\$4.50}$$

**b)** If a \$120 bike is reduced by 25%, what is the discount?

*discount:*

$$= \quad = \boxed{\$}$$

**c)** If a \$500 computer is reduced by 25%, what is the discount?

*discount:* 25% of 500 =

$$= \quad = \boxed{\$}$$

**d)** If an \$80 game is reduced by 40%, what is the discount?

*discount:*

$$= \quad = \boxed{\$}$$

**e)** If a \$3000 laptop is reduced by 20%, what is the sale price?

*discount:* 20% of 3000 =

$$= \frac{20}{100} \times \frac{3000}{1} = 600 \quad \text{Divide by 100}$$

*sale price:* \$3000 - \$600 =  $\boxed{\$}$

**f)** If a \$500 dress is discounted by 40%, what is the sale price?

*discount:*

$$=$$

*sale price:*  $\quad = \boxed{\$}$

**g)** In a store a \$125 skirt is marked '50% off'. What is the sale price of the skirt?

*discount:*

$$=$$

*sale price:*  $\quad = \boxed{\$}$

**h)** In a store a \$240 suitcase is marked '10% off'. What is the sale price of the suitcase?

*discount:*

$$=$$

*sale price:*  $\quad = \boxed{\$}$

- i) If a \$400 gold bracelet is discounted by 30%, what is the sale price?

discount:

=

sale price:

=

\$

- j) If a \$25 000 car is reduced by 10%, what is the sale price?

discount:

=

sale price:

=

\$

- k) In a store a \$900 canoe is labelled 'Save 60%'. What is the sale price of the canoe?

discount:

=

sale price:

=

\$

- l) In a store a \$300 pram is labelled 'Save 15%'. What is the sale price of the pram?

discount:

=

sale price:

=

\$

- m) A printer is priced at \$200. Which is the better deal?

- A) 20% off  
B) \$50 cash back

sale price A:

=

sale price B:

=

⇒

- n) A watch is priced at \$450. Which is the better deal?

- A) Save 30%  
B) Take \$100 off

sale price A:

=

sale price B:

=

⇒

- o) A utility is priced at \$15 000. Which is the better deal?

- A) 10% discount  
B) Reduce by  $\frac{1}{5}$

sale price A:

=

sale price B:

=

⇒

- p) A lounge suite is priced at \$6000. Which is the better deal?

- A) Save 25%  
B) Reduce by  $\frac{1}{3}$

sale price A:

=

sale price B:

=

⇒



EITHER

- Change the percentage to a fraction out of 100.

Example:  $150\% = \frac{150}{100}$

- Rewrite the question as a multiplication (change “of” to “×”).
- Change the whole number to a fraction over 1.

Example:  $7 = \frac{7}{1}$

- Cross simplify the fractions before multiplying. (see skill 10.4, page 60)

OR

- First find 100% or other multiples of 100%.
- Then find the remaining percentage.
- Add the results.

To find  $200\% = \frac{2}{1} \Rightarrow$  multiply by 2  
 $300\% = \frac{3}{1} \Rightarrow$  multiply by 3

Q.  $350\%$  of  $40 =$

A.  $350\%$  of  $40 =$

OR

A.  $100\%$  of  $40$  is  $40$

So  $300\%$  is triple that, or  $120$

$50\%$  of  $40$  is  $20$

So  $350\%$  of  $40$  is

$120 + 20 = 140$

$= \frac{350}{100} \times \frac{40}{1}$  *Simplify: ÷ 10, twice*  
 $= 35 \times 4$   
 $= 140$

a)  $200\%$  of  $60 =$

$= \frac{200}{100} \times \frac{60}{1}$  *Simplify: ÷ 10, twice*

$= 20 \times 6 = 120$

b)  $300\%$  of  $50 =$

$=$    
 $=$

c)  $400\%$  of  $70 =$

$=$    
 $=$

d)  $120\%$  of  $80 =$  *Find 100%*

$100\%$  of  $80 = 80$

$20\%$  of  $80 = 16$  *Find 20%*

*Add the results*  
 $80 + 16 =$

e)  $110\%$  of  $90 =$

$=$    
 $=$

f)  $250\%$  of  $30 =$

$=$    
 $=$

g)  $250\%$  of  $40 =$

$= \frac{250}{100} \times \frac{40}{1}$   
 $= 25 \times 4 =$

h)  $140\%$  of  $50 =$

$=$

i)  $220\%$  of  $80 =$

$=$

j)  $130\%$  of  $60 =$

$=$

k)  $120\%$  of  $70 =$

$=$

l)  $350\%$  of  $40 =$

$=$

## Skill 11.7 Writing one number as a percentage of another number.

MM4.2 11 22 33 44  
MM5.1 11 22 33 44

- Form a fraction using the two numbers.

EITHER

- Multiply this fraction by 100%.
- Simplify the resulting fraction and/or change it to a mixed number if necessary. (see skill 9.1, page 41)

OR

- Find an equivalent fraction with the denominator 100, by multiplying or dividing both the numerator and denominator by the same number.
- Write this fraction as a percentage. (see skill 12.11, page 92)

*Hint: Both numbers must represent the same unit of measurement.*

### Multiplying by 100%

$$100\% = 1$$

Multiplying by 1 or 100% does not change the value.

**Q.** Write as a percentage: 23 out of 50.

**A.**  $23 \text{ out of } 50 = \frac{23}{50} \times 100\%$

$$= \frac{23}{50} \times \frac{100}{1}\%$$

*Simplify:  $\div 50$*

$$= \frac{23}{1} \times \frac{2}{1}\%$$

$$= 23 \times 2$$

$$= 46\%$$

**OR**

**A.**  $23 \text{ out of } 50 = \frac{23}{50} \times 2$

$$= \frac{46}{100}$$

$$= 46\%$$

- a)** Write as a percentage:

12 out of 60.

$$\frac{12 \div 12}{60 \div 12} = \frac{1}{5}$$

*Simplify:  $\div 12$*

*Find equivalent fraction*

$$\frac{1 \times 20}{5 \times 20} = \frac{20}{100}$$

**20%**

- b)** In Australia 88 out of every 100 people live in an urban area. What percentage is this?
- .....
- .....

- c)** At the 2010 Delhi Commonwealth Games, 3 out of the 4 medals won by Samoa were gold. What percentage is this?
- .....
- .....
- =

- d)** For every 20 Skype calls made, 8 calls are video to video. What percentage is this?
- .....
- .....

- e)** A male lion weighs 225 kg. It eats 9 kg of food each day. What percentage of its own weight does a lion eat each day?
- .....
- .....
- 

- f)** Of the 1 billion cattle in the world, 200 million are in India. What percentage of the world's cattle are in India?
- .....
- .....
-

- Calculate the profit or the loss, as the difference between the selling and the cost price.
- Express the profit or the loss as a percentage of the cost price. (see skill 11.7, page 76)

**Q.** A shop buys jackets in bulk for \$50 each, then sells them for \$95 each. Calculate the profit on each jacket as a percentage of the cost price.

**A.** *profit:*  $\$95 - \$50 = \$45$   
*profit out of cost price:*  $\$45 \text{ out of } \$50 = \frac{45}{50}$   
 $= \frac{45}{50} \times \frac{100}{1} \% = \frac{450}{5} \%$   
 $= 90\%$

**a)** Lorien lost \$40 on a ring costing \$400. What was her loss as a percentage of the cost price?

*loss:* \$40

*loss out of cost:* \$40 out of \$400 =

$= \frac{40}{400} \times \frac{100}{1} \% = \frac{40}{4} \% = \boxed{10\%}$

**b)** The Cycle Centre made \$30 profit on a bicycle costing \$150. What was the profit as a percentage of the cost price?

*profit:*

*profit out of cost:*

=

**c)** John made \$20 profit on a tool box costing \$100. What was his profit as a percentage of the cost price?

*profit:*

*profit out of cost:*

=

**d)** Jason lost \$15 on a book costing \$30. What was his loss as a percentage of the cost price?

*loss:*

*loss out of cost:*

=

**e)** Serena bought a car for \$5000. If she later sold it for \$3500, find the loss as a percentage of the cost price.

=

**f)** A shop buys school uniforms in bulk for \$75 each, then sells them for \$100 each. Find the profit as a percentage of the cost price.

=

**g)** Amelia bought a table for \$400. If she later sold it for \$350, find the loss as a percentage of the cost price.

=

**h)** A painting was bought for \$6000. If it was later sold for \$7500, find the profit as a percentage of the cost price.

=

