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<b>1.</b>		<b>[Long <math>\times, \div</math>]</b> .....	<b>1</b>
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	1.2	Multiplying a large number by a two-digit number.	
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	1.4	Dividing a large number by a single digit.	
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	3.4	Multiplying a decimal number by a decimal number.	
	3.5	Dividing a decimal number by a whole number.	
	3.6	Dividing a decimal number by a power of 10.	
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	4.7	Adding fractions with different denominators - the HCF of the denominators is 1 (e.g. 2 and 3, 5 and 6).
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MM	SB	[Maths Mate - Mathematical strand]	
Question	Skill No.	Skill Builder - Skill description	
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